Estimating neurotransmitter kinetics with ntPET: A simulation study of temporal precision and effects of biased data

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We recently introduced neurotransmitter PET (ntPET), an analysis technique that estimates the kinetics of stimulus-induced neurotransmitter (NT) release. Here, we evaluate two formulations of ntPET. The arterial (ART) approach measures the tracer input function (TIF) directly. The reference (REF) approach derives the TIF from reference region data. Arterial sampling is considered the gold standard in PET modeling but reference region approaches are preferred for reduced cost and complexity. If simulated PET data with unbiased TIFs were analyzed using ART or REF, temporal precision was better than 3 min provided NT concentration peaked less than 30 min into the scanning session. The consequences of biased TIFs or stimulus-induced changes in tracer delivery were also evaluated. ART TIFs were biased by the presence of uncorrected radiometabolites in the plasma whereas REF TIFs were biased by specific binding in the reference region. Simulated changes in tracer delivery emulated ethanol-induced blood flow alterations observed previously with PET. ART performance deteriorated significantly if metabolites amounted to 50% of plasma radioactivity by 60 min. The accuracy and precision of REF were preserved even if the reference region contained 40% of the receptor density of the target region. Both methods were insensitive to blood flow alterations (proportional changes in $K_1$ and $k_2$). Our results suggest that PET data contain information – heretofore not extracted – about the timing of NT release. The REF formulation of ntPET proved to be robust to many plausible model violations and under most circumstances is an appropriate alternative to ART.

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release elicited by a drug may be a strong indicator of the drug’s addictive liability and potential for abuse (Spencer et al., 2006; Volkow et al., 1995, 1999; Volkow and Swanson, 2003). Boileau et al. (2007) speculated that amphetamine- and placebo-induced dopamine responses may follow distinct time courses, but noted that PET was not capable of distinguishing such differences. An imaging-based method for measuring the temporal profile of NT release, with sufficient resolution and accuracy, would constitute a new tool for addressing such speculations and for evaluating drug action more broadly.

Dynamic PET data reflecting the uptake and retention of receptor tracers has been modeled successfully with the two-tissue compartment model (Mintun et al., 1984). In applying the two compartment model to the data, one assumes a constant concentration of any competitor, such as an endogenous NT. More complicated models (Endres et al., 1997; Morris et al., 1995) have been introduced to accommodate time-varying concentrations of endogenous species. With these models, one can predict the effect of a transient increase in NT level on the dynamic PET data. These models necessarily require more parameters than the Mintun model.

To estimate more than the four parameters of the standard model from PET data, some investigators have tried to increase the information content of the data by experimental manipulation of the system. Along these lines, multiple injections of tracer at different specific activities have been administered during a single scan session (Christian et al., 2004; DeLorge et al., 1989, 1990; Huang et al., 1989; Miller et al., 2000; Morris et al., 1996a,b; Muzic et al., 1996). Multiple injection approaches facilitate observation of the system at multiple operating points; model fitting of all the data simultaneously leads to improved identifiability of parameters. Our implementation of ntPET can be seen as an extension of the multiple injection concept to a two-scan protocol in which we manipulate the implementation of ntPET can be seen as an extension of the multiple injection approach rather than the concentration of unlabeled tracer. Data from both scan conditions are analyzed simulations of NT release accompanied by blood flow. The ART and REF variants of ntPET derive their respective TIFs from different measurements, so the relevant model violations that we investigated were necessarily different. To test the robustness of the ART method, we supplied it with arterial plasma curves that were not corrected for the presence of labeled polar metabolites. To test the REF method, we provided it with PET data from non-ideal reference regions that contained receptors. To test the effects of activation-induced changes in tracer delivery, we analyzed simulations of NT release accompanied by blood flow changes and also simulations of flow changes alone. The precise nature of activation-induced alteration of tracer delivery and its impact on blood flow parameters (i.e., $K_1$ and $K_2$) remains unclear (Alpert et al., 2003; Logan et al., 1994; Pappata et al., 2002), so multiple scenarios were examined. Based on our results, we offer recommendations on the practical application of the ART and REF formulations of ntPET, including the conditions under which the REF method could serve as an acceptable substitute for the more demanding, but perhaps more accurate, ART method.

Methods

Model development

The compartmental model used in ntPET (Morris et al., 1995), illustrated schematically in Fig. 1, is an extension of the standard two-tissue compartment model to include competition between the tracer and an endogenous NT at the receptor sites. Competitive binding is assumed because both tracer and NT bind specifically to receptors that are present in finite number. The model is composed of coupled mass balances for the tracer and the NT. The tracer can exist in three possible states (suspended in plasma, $C_T(t)$; free in tissue, $F(t)$; and bound to a receptor, $B(t)$), whereas the NT can exist as either free ($F^{NT}(t)$) or bound ($B^{NT}(t)$). The model rate constants represent the rate of transfer of a molecule between states. The rate constants are typically first order, although transition from the free state to the bound state is a bimolecular (and saturable) interaction between free ligand (i.e., tracer or NT)
and available (i.e., unoccupied) receptor. The mass balance for free tracer, \( F(t) \), is
\[
\frac{dF}{dt} = K_{1}C_{p}(t) - k_{2}F(t) - k_{on}[B_{\text{max}} - B(t) - B^{NT}(t)]F(t) + k_{off}B(t)
\]
(1)

where \( B_{\text{max}} \) is total receptor concentration, including receptors occupied by the NT. In the past, \( B_{\text{max}} \) was often used imprecisely to refer to the density of unoccupied receptors. However, the concentration of available receptors is more properly designated \( B_{\text{avail}} \) (Innis et al., 2007). The mass balance equation for bound tracer, \( B(t) \), is
\[
\frac{dB}{dt} = k_{on}[B_{\text{max}} - B(t) - B^{NT}(t)]F(t) - k_{off}B(t)
\]
(2)

and the balance for bound NT, \( B^{NT}(t) \), is
\[
\frac{dB^{NT}}{dt} = k_{on}^{NT}[B_{\text{max}} - B(t) - B^{NT}(t)]F(t) - k_{off}^{NT}B(t).
\]
(3)

The tracer and neurotransmitter generally do not demonstrate identical binding kinetics, therefore their respective association \( k_{on} \) and dissociation \( k_{off} \) rate constants are not the same. The state variables in Eqs. (1)–(3) have units of chemical concentration.

The output equation relates the compartment concentrations to the PET signal. The PET signal for a given time frame is the sum of the radioactive tracer states weighted by their respective volume fractions, integrated over the frame duration.
\[
\text{PET}_{i} = \frac{1}{\Delta t_{i}} \int_{t_{i}}^{t_{i}+\Delta t_{i}} e_{V}C_{WB}(t) + e_{F}[F(t) + B(t)]SA(t)dt
\]
(4)

The specific activity term, \( SA(t) \), converts the free and bound states from molar to radioactivity concentration; \( SA \) is time-varying due to radioactive decay. The whole blood volume fraction is \( e_{V} \), \( e_{F} \) is the tissue volume fraction, where \( e_{T} = 1 - e_{V} \). The midpoint and duration of the \( i \)th frame are \( t_{i} \) and \( \Delta t_{i} \), respectively. \( C_{WB}(t) \) is the whole blood radioactivity concentration.

The ntPET model contains two time-varying inputs. The TIF, \( C_{p}(t) \), is the concentration of tracer in the plasma. As mentioned above, the TIF is obtained either by directly sampling arterial blood or by deriving it from PET data in a reference region. The mass balance equation for a reference region (Eq. (1) with binding terms omitted) can be rearranged to yield an expression for \( C_{p}(t) \),
\[
C_{p}(t) = \frac{1}{k_{\text{REF}}^{1}} [\frac{dF_{\text{REF}}^{\text{NT}}(t)}{dt} + k_{2}^{\text{REF}}F_{\text{REF}}^{\text{NT}}(t)]
\]
(5)

Thus, the TIF can be approximated from the time course of the free tracer in the reference region and its time derivative, provided \( k_{1}^{\text{REF}} \) and \( k_{2}^{\text{REF}} \) are estimated with the other model parameters.

The second model input is \( F^{NT}(t) \), the concentration of free NT in the tissue. In the present implementation, the time-varying free NT is parameterized as a gamma variate function,
\[
F^{NT}(t) = \text{Basal} + \gamma(t - t_{0})^{e_{\text{F}} - \epsilon(t - t_{0})}
\]
(6)

\( \text{Basal} \) is the baseline neurotransmitter concentration prior to perturbation. The magnitude of the response is scaled by \( \gamma \); the steepness of ascent and descent are dictated by \( \alpha \) and \( \beta \), respectively. The effect of each parameter on the gamma variate function is demonstrated in Fig. 2. These NT parameters comprise the elements of the vector \( \Theta \) (\( \text{C}_{\epsilon} \)). Mathematically, \( F^{NT}(t) \) is an input to the model; physiologically, it is the endpoint that we seek. Since
it cannot be measured directly, we must estimate it from the PET data. The timing of the NT response is our primary interest, thus we consider the key characteristics to be delay time, $t_d$; peak time, $t_p = t_d + \alpha / \beta$; and peak height, $F_{NT}(t_p)$.

The tracer and NT parameters are estimated by simultaneously fitting the model to dynamic PET data acquired during the rest and activation conditions. We assume that tracer parameters are identical in both conditions, whereas the parameters describing NT dynamics are allowed to vary from baseline in the activation condition only.

**Computer simulations of PET data**

All programming was done in MATLAB (Mathworks, Inc., Natick, MA); the model was implemented using the COMKAT library of functions (Muzic and Cornelius, 2001). Three different types of data were simulated: (I) noisy TIFs, not biased by model violations; (II) noisy TIFs, biased by model violations; and (III) change in blood flow constant(s) during activation.

**Unbiased TIFs, no alteration in tracer delivery**

A canonical set of tracer parameters ($\Theta_{tr} = [K_1, k_3, k_{ov}, k_{off}, B_{max}]^T$) was chosen to match the cerebral pharmacokinetics of the PET radioligand $[^{11}C]$raclopride, a dopamine D$_2$/D$_3$ receptor antagonist. We targeted a resting BP of approximately 2.0 in creating our simulations. NT parameters (Eq (6)) were selected such that the shape of $F_{NT}(t)$ resembled the release of dopamine (DA) in response to cocaine (based on Volkow et al., 1999; see development in Yoder et al., 2004), a drug known to cause acute elevation of synaptic DA concentration. The magnitude of $F_{NT}(t)$ (peak value at 200% of baseline) was chosen to yield a change in blood flow constant(s) during activation.

**Biased TIFs, ART method**

To test the ART method, the input function used for simulation of data was subjected to first order metabolism such that unmetabolized (native) tracer accounted for either 80% (slow metabolism), 50% (moderate metabolism), or 10% (fast metabolism) of the total plasma radioactivity at the end of the scan period. The TIF to be used for parameter estimation (i.e., analysis), however, was taken to be the total plasma signal without correction for labeled metabolites. Thus, the input function for ART estimations was a corrupted version of the true TIF. Tracer metabolites were taken to be polar molecules and unable to cross the blood–brain barrier, so tests of REF, which uses only tissue TACs, did not consider this violation. 450 activation (3 metabolism rates × 6 delay times × 25 tracer parameter sets; see Table 1 lines 8–13 and 15–20) and 150 null (3 metabolism rates × 50 tracer parameter sets; see Table 1 lines 14 and 21) data sets were generated as described above.

The effect of metabolism on the time course of tracer in the plasma is illustrated in Fig. 3. The concentration of native tracer diminishes more quickly with higher rates of metabolism (Fig. 3A). The rate of metabolism does not change the total plasma radioactivity, but as metabolism progresses, a decreasing proportion of the plasma signal represents native tracer. By not correcting for the accumulation of labeled metabolites, we introduced a nonlinear bias to the TIF that increased with scan time and speed of metabolism. Fig. 3B shows an example of a noisy, simulated TIF, derived from total plasma radioactivity without correction for metabolites.

For all simulations in this category, $\Delta BP$ from data sets with NT release were smaller the more rapid the metabolism (Fig. 3A). The rate of metabolism does not change the total plasma radioactivity, but as metabolism progresses, a decreasing proportion of the plasma signal represents native tracer. By not correcting for the accumulation of labeled metabolites, we introduced a nonlinear bias to the TIF that increased with scan time and speed of metabolism. Fig. 3B shows an example of a noisy, simulated TIF, derived from total plasma radioactivity without correction for metabolites.

**Biased TIFs: REF method**

Data sets were generated with non-ideal reference regions (i.e., having non-zero receptor density) to test the REF method. Specifically, we considered reference-to-target receptor density ratios (RD$_{R,t}$) of 1:20, 1:10, 1:5, and 2.5. These conditions violated the central assumption of all reference region approaches,
namely, that the reference region is devoid of specific binding. ART does not use reference region data, so testing of ART did not consider this violation. NT release during activation was confined to the target region. 600 activation (4 different RDRR:T × 6 delay times × 25 sets of tracer parameters; see Table 1 lines 22–27 and 29–34) and 200 null (4 different RDRR:T × 50 sets of tracer parameters; see Table 1 lines 28 and 35) data sets were generated as described above.

Fig. 4 shows examples of reference region TACs containing specific binding and the TIFs derived from them. Fig. 4A confirms that increasing receptor density increases retention of tracer in the reference tissue. Following the initial peak, the scale of the biased TIFs reflects the degree of retention in the reference TACs, as shown in Fig. 4B.

Tracer binding in the reference region caused a negative bias in BP, as has been noted previously (Asselin et al., 2007; Slifstein et al., 2000). In turn, ΔBP of our simulated data was smaller the greater the reference region receptor density. ΔBP from null data was very small and was not dependent on the amount of reference region binding (see Table 1, lines 28 and 35).

Altered tracer delivery

Changes in blood flow or initial tracer uptake constants (i.e., $K_1$ and $K_1^{REF}$) as a result of activation would constitute a violation of

\[
\alpha/\beta \text{ indicates the latency between time of NT response onset (t_D) and time of NT response peak (t_P = t_D + \alpha/\beta). Measured } \Delta BP \text{ is the change in binding potential calculated from the simulated time–activity curves by graphical analysis with reference region input. False classification rate is the fraction of false positive or false negative events as determined using the 95% confidence threshold obtained from analysis of noisy null data sets with no model violations.}
\]
the assumption that kinetic rate constants (i.e., the elements of $\Theta_{TR}$) are time-invariant. We addressed four possible stimulus-induced alterations of tracer delivery based on the effects of an ethanol challenge (Volkow et al., 1988): (1) decrease in blood flow to the reference region ($BF_{REF}$), (2) decrease of $K_1^{REF}$ by 10%, (3) increase in blood flow to the target region ($BF_{TAR}$) concurrent with decreased $BF_{REF}$, and (4) increase of $K_1$ by 10% concurrent with decrease of $K_1^{REF}$ by 10%. To simulate decreased $BF_{REF}$, both $K_1^{REF}$ and $k_2^{REF}$ were lowered by 10%. To simulate increased $BF_{TAR}$, both $K_1$ and $k_2$ were increased by 10%. In each case, alteration of tracer delivery started 15 min after the start of the activation scan and persisted for the remainder of the scan. The change in parameter(s) was implemented by simulating the data in two distinct epochs. First, data were simulated in the conventional manner (i.e., with
zero initial conditions) up to the time at which blood flow or $K_1$ changed. Then, using the state variables from the end of the first epoch as the initial conditions for the second epoch, data were simulated with the blood flow parameter(s) at new, constant value(s) for the remainder of the scan. All four alterations of tracer delivery were simulated both with and without NT response.

Fig. 5 shows noiseless examples of simulated TACs containing altered tracer delivery. In Fig. 5A, TACs in the rest condition are overlaid on TACs generated with an increase of $BFTAR$ and a decrease of $BREF$ beginning at 15 min. For both regions, TACs with changes in blood flow were nearly indistinguishable from TACs from those in the rest condition. In Fig. 5B, the same comparison is made for increased $K_1$ and decreased $K_{REF}$. The change began at 15 min and there was no NT response. TACs simulated with changes in $K_1$ or $K_{REF}$ were shaped differently than those without activation-induced artifact.

Simulations including changes in blood flow had $\Delta BP$ values similar to equivalent simulations without flow artifacts (Table 1, lines 36–39). Simulations with altered $K_1$ or $K_{REF}$ and NT release were characterized by markedly lower $\Delta BP$ (Table 1, lines 40 and 42). Null data sets with altered $K_1$ or $K_{REF}$ gave negatives values for measured $\Delta BP$ (Table 1, lines 41 and 43).

**Application of ART and REF methods**

**Parameter estimation**

Parameter estimation was performed using penalized weighted non-linear least squares. The objective function was composed of the weighted residual sum of squares from the rest and activation conditions and two penalty terms. The first penalty term constrained the time of peak NT concentration ($t_P-t_\alpha+\delta/\beta$) during activation. The second penalty constrained binding potential ($BP=k_{on}[B_{max}-B^*]/k_{on}$) during rest. The penalized objective function was

$$
\Phi(\Theta_{TR},\Theta_{NT}) = \sum w_i \left[ \text{PET}_{meas}^i - \text{PET}(\Theta_{TR},\Theta_{NT}) \right]^2 \\
+ \tau_1 \exp\left[-(t_P(\Theta_{NT}) - t_i)\right] + \exp\left[(t_P(\Theta_{NT}) - t_i)\right] \\
+ \tau_2 \left[ BP_{meas} - BP(\Theta_{TR},\Theta_{NT}) \right]^2
$$

where $w_i$ are the weights applied to each residual (set proportional to $\sigma_i^{-2}$), and $\tau_1$ and $\tau_2$ are weights applied to the penalty terms ($t_P=60$), $t_\alpha$ and $t_\delta$ are the lower and upper peak time constraints ($t_\alpha=0$ min, $t_\delta=60$ min) and $\Theta_{TR}$ and $\Theta_{NT}$ are the vectors of tracer and NT parameters, respectively. For better performance, one could reasonably assume that the NT response is causal and set $t_\alpha$ to the time of stimulus onset, although we did not do that here. $BP(\Theta_{TR}, \Theta_{NT})$ is calculated from the estimated parameters on each iteration of the fitting procedure, whereas $BP_{meas}$ is determined independently by a graphical analysis (Logan et al., 1996) of the rest data prior to parameter estimation. Eq. (9) is minimized by parameters which fit the data from both scan conditions, yield a $BP$ near $BP_{meas}$, and find NT events which peak during the scan. For clarity, estimated quantities will be indicated by a caret (e.g., $t_\alpha$ is the delay time estimated from data; $t_\alpha$ is the true delay time used in simulations).

Noiseless TIFs were used to generate simulated data, but noisy TIFs were used in the estimation process. The noisy TIFs provided to ART for parameter estimation were produced by adding zero-mean Gaussian noise to the total plasma radioactivity signal. The TIFs used for REF analyses were derived (see Eq. (5)) from the noisy-simulated reference region data.

**Parameter identifiability, goodness of fit, and classification**

Due to the large number of parameters being estimated, correlation between parameters, and noise in the data, we were wary of possible dependence of our final estimates on the initial parameter guess. As a precaution, we fit each data set 50 times with 50 initial guesses chosen randomly from a uniform distribution across a wide range of parameter values. Refer to Fig. 6 for a plot of the 50 NT responses associated with a typical set of 50 initial guesses. Of the estimations that converged for a given data set, the best model fits to the data were determined by a multiple stage goodness of fit selection process based on objective criteria (Morris et al., 2005). In the first step, we eliminated fits with weighted residual sum of squares greater than the median. From the fits that were retained, we kept only the ones having at least as many runs (zero crossings in the residuals) as the median number. Therefore, analysis of each data set yielded multiple answers representing a group of NT responses that best explain the data from both scan conditions and two penalty terms. The first penalty term constrained the time of peak NT concentration ($t_P-t_\alpha+\delta/\beta$) during activation. The second penalty constrained binding potential ($BP=k_{on}[B_{max}-B^*]/k_{on}$) during rest. The penalized objective function was

$$
\Phi(\Theta_{TR},\Theta_{NT}) = \sum w_i \left[ \text{PET}_{meas}^i - \text{PET}(\Theta_{TR},\Theta_{NT}) \right]^2 \\
+ \tau_1 \exp\left[-(t_P(\Theta_{NT}) - t_i)\right] + \exp\left[(t_P(\Theta_{NT}) - t_i)\right] \\
+ \tau_2 \left[ BP_{meas} - BP(\Theta_{TR},\Theta_{NT}) \right]^2
$$

where $w_i$ are the weights applied to each residual (set proportional to $\sigma_i^{-2}$), and $\tau_1$ and $\tau_2$ are weights applied to the penalty terms ($t_P=60$), $t_\alpha$ and $t_\delta$ are the lower and upper peak time constraints ($t_\alpha=0$ min, $t_\delta=60$ min) and $\Theta_{TR}$ and $\Theta_{NT}$ are the vectors of tracer and NT parameters, respectively. For better performance, one could reasonably assume that the NT response is causal and set $t_\alpha$ to the time of stimulus onset, although we did not do that here. $BP(\Theta_{TR}, \Theta_{NT})$ is calculated from the estimated parameters on each iteration of the fitting procedure, whereas $BP_{meas}$ is determined independently by a graphical analysis (Logan et al., 1996) of the rest data prior to parameter estimation. Eq. (9) is minimized by parameters which fit the data from both scan conditions, yield a $BP$ near $BP_{meas}$, and find NT events which peak during the scan. For clarity, estimated quantities will be indicated by a caret (e.g., $t_\alpha$ is the delay time estimated from data; $t_\alpha$ is the true delay time used in simulations).

Noiseless TIFs were used to generate simulated data, but noisy TIFs were used in the estimation process. The noisy TIFs provided to ART for parameter estimation were produced by adding zero-mean Gaussian noise to the total plasma radioactivity signal. The TIFs used for REF analyses were derived (see Eq. (5)) from the noisy-simulated reference region data.
conditions (i.e., an “NT profile family”). Reported parameters (i.e., \(t^\text{D}\), \(t^\text{P}\), \(F^\text{NT}(t^\text{P})\)) for a single data set represent peak height, delay time, and peak time averaged over each member of the resultant NT profile family. Reported standard deviations (see Results) represent the variability in reported parameters from multiple data sets.

In the final post-processing step, the average peak height of the NT profile family was compared to a “95% confidence threshold” determined by analysis of null data without model violations. The threshold was set such that ntPET analysis of at least 95% percent of the null data sets yielded an average peak height less than the threshold. Because ART and REF yielded different results from the same data, each method was assigned its own threshold value (see Results section). A family of estimated NT responses which had an average peak height exceeding the threshold was considered a positive event. If the estimated NT profile family was from data containing a true NT response, the event was classified as a true positive; if the NT profile family was from null data, the event was designated a false positive. True negatives and false negatives were defined similarly.

Results

Unbiased TIFs, no alteration in tracer delivery

Null data

Analyses of null data via either method typically found little or no NT response. Fig. 7 shows a representative ART fit to null data and the estimated NT profile family. The NT responses estimated from null data were characterized by small peak height (112±10% of baseline for ART; 107±13% of baseline for REF) and large temporal variance (\(\sigma(t^\text{D})=10.78\) min, \(\sigma(t^\text{P})=9.69\) min using ART; \(\sigma(t^\text{D})=14.82\) min, \(\sigma(t^\text{P})=11.94\) min using REF). Over 95% of the NT profile families estimated by ART from null data had an average peak height less than 129% of baseline. Thus, we designated 129% of baseline as the “95% confidence threshold” for families of NT curves estimated from PET data at this noise level (\(\zeta=0.03\); see Eq. (7)). The 95% confidence threshold for the REF method based on these same data was 131%.

Data with NT response

An ART example fit to PET data and the estimated NT profile family are shown in Fig. 8. The average peak heights of the NT

Fig. 7. Example of results obtained from simulated null data by applying ART using a noisy, unbiased TIF. Left panels (A, B): simulated PET data (open circles), measured plasma input (black circles), and model fit to the data (solid black curve). Right panels (C, D): estimated NT responses (black curves) from different initial parameter guesses. Top panels (A, C) refer to rest condition, bottom panels (B, D) to activation. There are 13 retained NT responses shown in D.
profile families estimated by both the ART and REF methods from simulated data with an authentic NT response typically exceeded the 95% confidence thresholds. All data sets analyzed by ART yielded NT response families with average peak heights exceeding the ART 95% confidence threshold. 149 of 150 NT profile families estimated by REF exceeded the REF 95% threshold. See Table 1 (lines 1–6) for a listing of false classification rates.

Fig. 9 presents the performance of the ART and REF methods for NT events occurring at different times during the scan session. In the upper and middle panels of Fig. 9, \( t_D \) and \( t_P \) estimated from 25 data sets containing the same true NT response for every delay time are plotted against their respective true values. \( F^{NT}(t_P) \) is plotted as a function of \( t_D \) in the bottom panel of Fig. 9. For comparison, ΔBP measured from the curves is also provided. Fig. 9 is based on unbiased TIFs only. For early NT release (\( t_D \leq 15 \) min), the ART method estimated delay time with slightly less bias than did REF; for later NT release, REF estimates of delay time were closer to the true values. ART and REF both overestimated peak time by several minutes, but ART generally showed slightly smaller bias. Peak height was consistently underestimated by both methods. Parameters estimated by ART tended to have slightly lower variance than those estimated by REF, particularly for early NT events.

Biased TIFs: Effect on ART method

Null data

Average peak heights of NT profile families estimated by ART from null data with slow tracer metabolism were 118±14% of baseline and 155±26% of baseline for moderate metabolism. The false positive rate for slow metabolism was 22% but jumped to 90% for moderate metabolism. Variance in timing parameters estimated from null data with slow metabolism was large (\( \sigma(t_D) = 16.17 \) min, \( \sigma(t_P) = 15.36 \) min). Moderate metabolism gave less temporal uncertainty than slow metabolism (\( \sigma(t_D) = 6.07 \) min, \( \sigma(t_P) = 4.81 \) min). The model was unable to fit the data when rapid metabolism of the tracer was uncorrected.

Data with NT response

Fig. 10 displays overall performance of the ART method in the presence of uncorrected metabolism. Delay time was accurately estimated if metabolism was slow but overestimated if it was moderate. Peak time was consistently overestimated with large variance for slow metabolism, but correlation with the true values was high (\( R^2 = 0.96 \)). Moderate metabolism prevented any meaningful estimation of peak time. For both rates of metabolism, variance in estimated peak height was greatest for late responses. Peak height was consistently underestimated by ART using biased TIFs. See Table 1 (lines 8–13 and 15–20) for the associated false negative rates.

Biased TIFs: Effect on REF method

Null data

The peak heights estimated by the REF method from null data with non-ideal reference regions were similar to those estimated using unbiased TIFs. The frequency of false positive events for RDRr:T 1:5 and RDRr:T 2:5 are reported in Table 1 (see lines 28
and 35). In no case was the false positive rate greater than 4%, nor did extent of receptor density in the reference region correlate with number of false positives. The estimated NT profiles were temporally incoherent; both $\sigma(t_{D})$ and $\sigma(t_{P})$ were greater than 10 min for all cases.

**Data with NT response**

Fig. 11 demonstrates the ability of the REF method to determine the NT profile if TIFs are biased. The two cases with greatest amounts of binding in the reference region, RDR$_{R,T}$ 1:5 and RDR$_{R,T}$ 2:5, are shown. Peak time is consistently overestimated but peak height estimates are not dependent on the timing of NT release. The rate of false negative findings was low and did not correlate with density of receptors in the reference region or with timing of NT response (see Table 1, lines 22–27 and 29–34). Variances of the estimated parameters were greater for later NT release, but generally similar to those observed using unbiased TIFs.

**Altered tracer delivery**

**Changes in blood flow**

**Null data.** For all cases, estimated NT profiles had consistently small magnitude and large temporal uncertainty. Peak height estimated by REF was $111\pm13\%$ of baseline when $BF_{REF}$

![Figure 9](image9.png)

*Fig. 9.* Values of key NT parameters (i.e., delay time, peak time, and peak height) estimated by ART and REF using unbiased TIFs. ART estimates are indicated by black curves and REF estimates by dashed gray curves. The line of identity is indicated by a thick dotted black line. Top panel pertains to delay time, middle panel to peak time, and bottom panel to peak height. Measured changes in BP, indicated by square symbols, are included on peak height plot for comparison.

![Figure 10](image10.png)

*Fig. 10.* Key NT parameters estimated by ART using biased TIFs. Estimates from data with slow metabolism are indicated by black curves and estimates from data with moderate metabolism by dashed gray curves. The line of identity is indicated by a thick dotted black line. Top panel pertains to delay time, middle panel to peak time, and bottom panel to peak height. Measured changes in BP (slow metabolism indicated by black squares, moderate metabolism by gray squares) are included on peak height plot for comparison.
null data

The NT profiles estimated from null data with altered $K_1$ or $K_{1\text{REF}}$ had very small peak height and large temporal variance. Fig. 12 shows a representative REF fit and the family of estimated NT profiles from null data that were simulated with a decrease in $K_{1\text{REF}}$ beginning at 15 min. Note that the model fit is poor (residuals are predominantly negative in the rest scan and positive in the activation scan) due to the incompatibility of the reference region TAC (and thus the TIF derived from it) in the activation condition with all other data. The NT curves estimated from null data sets containing decrease in $K_{1\text{REF}}$ are characterized by very small magnitudes, with average peak height 100±1% of baseline. REF analysis of null data sets yielded an estimated peak height 100±0% of baseline if $K_1$ increased and $K_{1\text{REF}}$ decreased. Peak height estimated by ART was 102±3% if initial uptake increased in the target region. No false positives were found in any of these cases (see Table 1, lines 41 and 43).

Data with NT response. Simulated changes in $K_1$ and/or $K_{1\text{REF}}$ alone exacerbated the underestimation of peak height from simulated data containing NT release. REF estimated the peak height to be 145±19% of baseline when $K_{1\text{REF}}$ decreased. If $K_1$ increased, peak height estimated by ART was 143±17%. REF estimates of peak height decreased considerably if $K_1$ increased and $K_{1\text{REF}}$ decreased. In this case, estimated peak height was 109±11%. False negative rates were large, particularly for $K_1$ increase with $K_{1\text{REF}}$ decrease (refer to Table 1, lines 40 and 42).

Alterations of $K_1$ and/or $K_{1\text{REF}}$ alone exhibited varied effects on the accuracy of estimated NT timing parameters. Fig. 13 shows a typical REF fit and the estimated NT profile family for the case of an NT response accompanied by a simultaneous decrease of $K_{1\text{REF}}$. The estimated NT curves are temporally coherent and resemble a slightly delayed version of the true response. Decreased $K_{1\text{REF}}$ increased the REF overestimation of delay time (bias(Δt$_0$)=-3.31 min vs. 1.33 min with no model violations). ART also overestimated delay time (bias (Δt$_0$)=2.44 min vs. -0.21 min with no model violations) when $K_1$ increased. $K_1$ increase with concurrent $K_{1\text{REF}}$ decrease caused REF to estimate both timing parameters inaccurately (bias(Δt$_0$)=-4.89 min, bias(Δt$_D$)=-4.60 min) and imprecisely (σ(Δt$_0$)=12.91 min, σ(Δt$_D$)=9.08 min).

Effects of altered tracer delivery on detection ability

We looked at a number of possible scenarios that involved alteration of blood flow parameters. To summarize the detection ability of the ART and REF models in the face of changes in blood flow parameters, we present detection results via receiver operating characteristic (ROC) curves. ROC curves for analyses of data with altered BF were shown in Fig. 14. Circles on the figure indicate our chosen operating point, based upon the 95% confidence thresholds obtained from null data with constant flow parameters and unbiased TIFs. Fig. 14A demonstrates that simulated changes in blood flow did not seriously compromise the detection ability of either the ART or the REF method. False
positive rates remained consistent with those from data with constant flow parameters. Fig. 14B shows the ability of each method to detect a true NT response if $K_1$ and/or $K_1^{REF}$ change during activation (but $k_2$ and $K_2^{REF}$ do not). Because the alterations in tracer delivery tended to decrease the height of the estimated NT profiles in the true activation and null cases, both the true positive and false positive rates were decreased. In fact, when $K_1$ increased and $K_1^{REF}$ decreased, 96% of true NT responses were below the 95% confidence threshold established for REF analysis.

Discussion

The present work examines the temporal precision of two variants of ntPET and assesses the performance of the methods when confronted with likely violations of model assumptions. In addition, we compare the ART and REF formulations and determine under what conditions the use of a reference region-derived TIF is an acceptable alternative to arterial blood sampling. We develop these ideas here, explore some technical details of the methods, and consider the complementary roles that ntPET and microdialysis could play in studying neurotransmission in vivo.

Temporal precision of ntPET

The temporal precision of ntPET varies slightly with the timing of the NT response. In general, performance is better when NT release occurs early rather than late in the scan. Absent model violations, the precision of estimated delay time, $t_D$, is approximately $\sigma(t_D) = 2$ min using ART and $\sigma(t_P) = 2.5$ min using REF for early NT events (defined as true $t_P = 15$ to 25 min); uncertainty of estimated peak time, $t_P$, is less than 2 min with ART and 2–2.5 min with REF. The error in estimated timing parameters tends to increase as the NT response occurs later in time. With the ART method, we find $\sigma(t_D) \approx 4$ min and $\sigma(t_P) \approx 4.5$ min when data have late NT responses (defined as true $t_P = 30$ to 40 min). Under similar conditions, the REF method estimates both timing parameters with comparable variance ($\sigma(t_D) \approx \sigma(t_P) \approx 3.5$ min). We have shown previously that the precision of estimated parameters improves with the prominence of the NT profile (i.e., larger magnitude and greater sharpness of the NT response, and higher PET signal-to-noise ratio) (Normandin and Morris, 2006).

The ability of ntPET to characterize NT dynamics represents a potential advance in PET analysis. The temporal resolution that we report here may be sufficient to provide answers that have previously eluded researchers. For instance, PET investigators have compared the kinetics of cocaine and methylphenidate (Volkow et al., 1995; Volkow et al., 1999) and the effects of long- and short-acting methylphenidate (Spencer et al., 2006), and surmised that the speed of their respective dopamine responses may predict their addictive liabilities. However, it would be impossible to test this hypothesis with PET by measuring change in binding potential. In recent work investigating conditioned NT release, Boileau et al. (2007) found that the change in raclopride binding potential after amphetamine was the same as after placebo, but the behavioral effects persisted longer after drug. They speculated that amphetamine- and placebo-induced dopamine responses may have distinct
temporal characteristics, but lamented the inability of PET to resolve such a difference. We believe that, coupled with an appropriate analysis technique, PET could discern different temporal profiles in NT responses. Answers to questions about the time course of NT release may be attainable through ntPET analysis.

Performance of ntPET under conditions of model violations

We examined plausible violations of model assumptions and evaluated their respective impacts on the results of ntPET. Many violations failed to undermine the method. The violations that did degrade model performance were either correctable (presence of...
labeled metabolites in the blood) or physiologically ambiguous (instantaneous changes in $K_1$ and/or $K_{1}^{REF}$ without accompanying changes in $k_2$ or $k_2^{REF}$).

**Uncorrected metabolites in blood**

The uncorrected presence of labeled metabolites in the plasma is a likely corruption of the measured TIFs used by ART. TACs decrease more quickly than they would otherwise, which could be attributed to faster tracer efflux or a sustained release of NT. This corruption of the input data causes a progressive bias with time and degrades the performance of ART. Therefore, when using the ART method, we recommend that metabolite correction be performed unless tracer metabolism is known to be very limited. Population-based corrections may not be adequate because rates of tracer metabolism can be highly variable between subjects (Gillings et al., 2001; Ishiwata et al., 1998) and can be influenced by drug metabolism can be highly variable between subjects (Gillings et al., 2001; Ishiwata et al., 1998) and can be influenced by drug metabolism. The previously demonstrated sensitivity of multiple tracer injection experiments to errors in the calculated input functions (Morris et al., 1999) supports this conjecture.

**Specific binding in reference region**

Reference region-derived TIFs could be biased by specific binding in the reference region, a common problem for non-dopaminergic NT systems (Litton et al., 1994; Logan et al., 2005) or for dopaminergic imaging with high-affinity tracers (Asselin et al., 2007; Christian et al., 2004; Delforge et al., 1999; Pinborg et al., 2007). The presence of receptors in the reference region increases tracer retention and, coupled with the errant assumption of no receptors, lends the appearance of lower than expected initial uptake in the target region than the reference region. This violation manifests itself as an underestimation of $R_1 = (K_1/K_{1}^{REF})$. Fortunately, the use of imperfect reference regions neither biases the temporal accuracy nor degrades the temporal precision of the REF method. Different amounts of specific binding in the reference region yield TIFs of different magnitudes but similar shape throughout most of the scan (see Fig. 4). In the present simulations of raclopride TACs, the derived TIF is dominated by the plateau that follows the early peak. Consistency in the shape of the resultant TIFs probably explains the insensitivity of REF to binding in the reference region.

**Flow parameters altered by activation**

Activation-induced changes in blood flow are likely to be encountered following many NT-releasing tasks. Such changes have been observed after ethanol administration using $\text{H}_2^{15}$O PET (Volkow et al., 1988). Our demonstration that alterations to the shapes of TACs caused by simulated changes in blood flow are negligible is in agreement with previous work (Alpert et al., 2003; Pappata et al., 2002), and any changes in the curves are well below the level of noise in typical data. Thus, changes in blood flow should not appreciably impact ntPET results.

If it were physiologically possible, alteration of $K_1$ and/or $K_{1}^{REF}$ alone could influence results obtained with ntPET. The trajectory of the target region TAC rises when $K_1$ is increased (see Fig. 5B). Release of NT has the opposite effect because it displaces the tracer from binding sites and lowers the TAC. When these two effects occur simultaneously they counteract one another, and the peak height of the NT response estimated by ART is attenuated. Similarly, a decrease of $K_{1}^{REF}$ reduces the magnitude of the NT responses estimated by REF. In these two cases, the sensitivity of ntPET is reduced but useful results may still be obtained. However, if $K_1$ is increased and $K_{1}^{REF}$ decreased, the NT responses estimated by REF will be completely nullified. To achieve greater sensitivity, one might consider lowering the threshold value. Unfortunately, even setting the threshold as low as 103% of baseline would yield a true positive detection rate of only 0.72. In addition, a low threshold would lead to an unacceptably large false positive rate (0.46) if the expected model violations did not occur. Thus, a modification of the threshold is not a viable correction to ntPET for the case of $K_1$ increase coupled with $K_{1}^{REF}$ decrease.

The physiological likelihood of isolated changes in $K_1$ remains unresolved (Alpert et al., 2003; Logan et al., 1994; Pappata et al., 2002). Nevertheless, our simulated tests with $K_1$ alterations represent worst case scenarios. Change in flow parameters may not coincide with NT release (Schwarz et al., 2004), and would probably depend upon the type of stimulus and might vary between individuals. With regard to our specific interest in alcohol-induced dopamine release, the simulated changes in $K_1$ and $K_{1}^{REF}$, which were chosen to simulate the alcohol-induced blood flow alterations reported by Volkow et al. (1988), should not cause false positive findings; rather, false negatives would result (refer to Fig. 14 and lines 40 and 42 of Table 1). Thus, any supra-threshold NT profiles estimated from data in subjects receiving alcohol could be confidently attributed to NT release. In practice, the threshold value may be established based on evaluations of rest–rest studies (the experimental null case) and/or simulations that appropriately represent the acquired data.

**Comparison of ART and REF**

The ART formulation of ntPET performs slightly better than REF, provided that (1) NT responses occur early in the scan, (2)
unbiased TIFs are available, and (3) the PET data are free of activation-induced changes in tracer delivery. Fig. 15 summarizes the respective performance of the methods by plotting the average estimated peak height against the average estimated peak time for ART and REF analyses of each data set that does not contain model violations. The points cluster more tightly for ART (shown at left) than REF, particularly for early NT events (darker markers). The performance advantage of ART over REF is less evident if NT responses occur later in the scan.

The two variants of ntPET behaved very differently when presented with realistically biased TIFs: ART performance deteriorated even with slow tracer metabolism, but REF was insensitive to specific binding in the reference region. Neither method was appreciably impaired by an activation stimulus that also caused a change in blood flow. A strength of the ART method is that it requires PET data from the target region only, whereas REF needs data from the target and a reference region. Thus, biases in either region could theoretically cause artifacts in REF analyses. If biases are present in both regions and in opposite directions (e.g., $K_1$ increases and $k_{11}^{\text{REF}}$ decreases) the impact on REF is severe. On the other hand, should the biases occur in the same direction (e.g., a “global” change in $K_1$), the REF method performs better than ART because the kinetic artifacts in the two regions counteract one another (data not shown). In other words, a global change in $K_1$ leads to a reference region-derived TIF that is consistent with the target region TAC, whereas the plasma curve is not. Unless the investigator specifically expects that the particular stimulus will increase $K_1$ and decrease $k_{11}^{\text{REF}}$ (or vice versa), we recommend the REF variant of ntPET as an alternative to ART that is more convenient, nearly as precise, and more robust to plausible corruptions of the TIF.

**Technical details**

**Peak time constraint**

Use of the peak time constraint marks an improvement over our original implementation of ntPET (Morris et al., 2005). This penalty term increases the value of the cost function if the peak of the NT response occurs outside the scan window. The peak time constraint has little effect if NT release peaks during PET acquisition, but it has a useful impact if there is no NT response (i.e., null data). If the peak time constraint were not used, the fitting routine would be free to find NT responses that peak before or after the scan. Since there are no data at these times to dictate the amplitude of the response, the estimated NT profiles could have very large magnitude. The net effect, if we included peaks outside the scan window, would be to force a higher 95% confidence threshold (based on null data), and thus accept more false negative events from data with bona fide NT responses.

**Characteristics of estimated peak height**

Peak height is consistently underestimated, as demonstrated by Fig. 8 and lower panels of Figs. 9–11. Absolute scale is not identifiable, but fractional scale (relative to basal NT level) can be determined. Peak height estimates have greater variability than do the timing parameters, particularly for early NT responses (see Fig. 15). Previous work (Normandin and Morris, 2006) has shown that underestimation of peak height is also observed with larger NT responses, but that the estimated peak height correlates with the true value. Although peak height is underestimated, the bias tends to be fairly consistent across a wide range of NT response times (see bottom panel of Figs. 9–11). This consistency contrasts with estimates of $\Delta BP$, which have been shown to be conflated with NT timing (Morris and Yoder, 2007; Yoder et al., 2004; see also bottom panels of Figs. 9–11). Because $PNT(\hat{t}_p)$ does not vary with NT response time, the peak height estimated by ntPET may be a more consistent measure of the magnitude of NT release than the commonly used $\Delta BP$.

**Parameter estimation, restrictions, and identifiability**

Parameter estimation was performed using the MATLAB function ‘lsqcurvefit’, a Levenberg–Marquardt algorithm. Convergence tolerances for function and parameter values (‘TolFun’ and ‘TolX’, respectively, in MATLAB optimization settings) were both set to $10^{-9}$. A given fit was terminated and considered non-converging if the number of iterations reached 400.

In the present studies, we have fixed $B_{\max}, k_{NT}^P$, and $k_{NT}^{\text{REF}}$ (Fisher et al., 1995; Morris et al., 1995), and restricted $\gamma$ to nonnegative values in order to detect only increases in NT. Future work to improve the practicality of the method will include efforts to reduce computational load and sensitivity to initial guess by fixing more parameters. This may be possible given sufficient preliminary data for a given tracer (i.e., prior knowledge of $\Theta_{TR}$).

We acknowledge that identifiability of parameters is a potential problem. We have sought to address this concern by using a constrained optimization routine that aids identifiability and by fitting the data with many different, randomly selected initial guesses. Our results with multiple initial guesses demonstrate that while a unique, global minimum in parameter space may not be attainable, the recovered neurotransmitter responses are generally consistent for a given data set. Note that this consistency is in stark contrast to the neurotransmitter profiles associated with the initial parameter guesses, examples of which are shown in Fig. 6. It should also be emphasized that the neurotransmitter timing parameters are largely insensitive to the choice of tracer parameters. Finally, we reiterate that the goal of ntPET analysis is the determination of the neurotransmitter profile; that is, for our purposes, the tracer parameters can be considered “nuisance” parameters.

**ntPET as a complement to microdialysis**

ntPET shares a common goal with microdialysis, namely, characterization of the time course of neurotransmitter concentration. Microdialysis is used extensively in neurochemical studies on animals, but requires placement of probes into the brain for direct assay of chemical species. Though ntPET and microdialysis are similar in their objective, their respective endpoints are dissimilar. For example, amphetamine and methylphenidate have been shown to cause comparable changes in intrasynaptic dopamine (as determined by $\Delta BP$ from PET) but different effects on extracellular dopamine (measured by microdialysis) (Schiffer et al., 2006b). Microdialysis samples from the extracellular fluid, whereas the PET signal and a proper model measure the effects of intrasynaptic binding and displacement of tracer. ntPET cannot be readily performed on awake rodents or provide sequential measurements over several days as can be done with microdialysis. On the other hand, ntPET is non-invasive and can be performed on humans. The collateral effects of microdialysis on brain physiology have recently been questioned, particularly with regard to probe-induced damage to tissue integrity (Bungay et al., 2003; Tang et al., 2003), cerebral metabolism (Frumberg et al., 2007; Schiffer et al., 2006a),...
and animal behavior (Fruminberg et al., 2007). These alterations will not be caused by ntPET. Nevertheless, ntPET and microdialysis may represent complementary techniques to resolve difference between intra- and extrasynaptic neurotransmitter fluctuations. If the relationship between microdialysis and ntPET can be determined, the vast microdialysis literature could be mined to suggest a large number of informative, translational studies in human subjects.

Conclusions

This simulation study evaluated two alternative formulations of ntPET under idealized conditions (noisy but unbiased data) and when confronted with plausible model violations. The ART formulation of ntPET, which obtains the tracer input function from arterial blood samples, was sensitive to the presence of labeled metabolites in the plasma that were left uncorrected. The REF variant of ntPET, which derives the tracer input function from reference region PET data, was robust to specific binding in the reference region. Neither ART nor REF was significantly influenced by changes in blood flow. However, the performance of both methods was impaired by changes in $K_i$ decoupled from changes in $K_t$. The accuracy of conventional ABP measurements was also degraded by changes in $K_t$. ABP is known to be compromised by the timing of NT release, whereas ntPET proved to be robust. Under most circumstances, the REF formulation of ntPET is an appropriate alternative to the more demanding ART method.

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